

Murnaghan fit

$$E = x(1) + x(3) \cdot V \cdot \frac{1}{x(4)[x(4)-1]} \left\{ x(4) \left[1 - \frac{x(2)}{V} \right] + \left(\frac{x(2)}{V} \right)^{x(4)} - 1 \right\}$$

$\begin{matrix} \uparrow & \uparrow & \uparrow & \uparrow \\ p_1 & p_2 & p_3 & p_4 \end{matrix}$

$$\frac{\partial E}{\partial V} = \frac{p_2}{p_3} \left[1 - \left(\frac{p_4}{V} \right)^{p_3} \right]; \quad \frac{\partial E}{\partial V} = 0 \Rightarrow \boxed{p_4 = V_{eq.}}$$

$$\frac{\partial^2 E}{\partial V^2} = \frac{p_2}{V} \left(\frac{p_4}{V} \right)^{p_3}$$

$$B = p_2 \left(\frac{p_4}{V} \right)^{p_3}; \quad \frac{\partial E}{\partial V} = 0 \Rightarrow$$

$$\boxed{p_2 = B.}$$

$$P = -\frac{p_2}{p_3} \left[1 - \left(\frac{p_4}{V} \right)^{p_3} \right]; \quad P = -\frac{p_2}{p_3} + \frac{1}{p_3} B;$$

$$B = p_2 + p_3 P;$$

$$\boxed{B' \equiv \frac{\partial B}{\partial P} = p_3}$$

$$\boxed{E(V_{eq.}) = p_1}$$

Conversion: p_2 from the fit is in $\left[\frac{R_y}{(\text{a.u.})^3} \right];$

$$\boxed{B = -V \frac{\partial P}{\partial V} = V \frac{d^2 E}{dV^2}}$$

Conversion: p_2 from the fit is in $\left[\frac{R_y}{(\text{a.u.})^3} \right]$,

$$1 \frac{R_y}{(\text{a.u.})^3} = \frac{\overbrace{13.61}^{\text{eV}/R_y} \times \overbrace{1.60219 \cdot 10^{-19}}^{\text{J/eV}} \text{ J}}{\underbrace{0.529177^3}_{\text{\AA}/\text{a.u.}} \cdot 10^{-30} \text{ m}^3} =$$

$$= \frac{13.61 \times 1.60219}{\underbrace{0.529177^3}} \cdot 100 \cdot 10^9 \frac{\text{N}}{\text{m}^2} =$$

$$= 14715.3 \text{ GPa}$$

$$= 147153 \text{ KBar}$$

Exp. values of B at room temperature:

Fe	1683 kbar	→
Mn	596	
Al	722	
Cu	1370	
Ni	1860	
Ti	1051	

Calculation for Fe:

2097	(TBLMTO)
2166	(WIEN-LDA)
1699	(WIEN-GGA)

$$1 \text{ bar} = 10^5 \text{ Pa}$$

$$1 \text{ kbar} = 0.1 \text{ GPa}$$